Computer Science 1 Bh

Degree Examination
Specimen Solutions

Date: Saturday 25th May 2002
Time: 12:00–13:30 (one and a half hours)
Place: Adam House
Room: Ground Floor

Board of Examiners
Chair: D.K. Arvind
External Examiner: R. Dyckhoff

Notes about Specimen Solutions

1. These specimen solutions are issued for guidance only, to help as a revision aid. They do not represent a complete picture of how the exam was marked; they are specimen solutions, not a marking guide.

2. The solutions typically present one answer from a set of possible answers. Often, answers which have alternative wording or different technical details are equally acceptable.

3. If you have any questions concerning these solutions, please contact the course organiser. Please note that the course organiser will not be able to answer questions about the marking of the exam.
**Question 1**

(a) A useful technique when building large systems is the ability to hide parts of the system from the view of other parts. Java provides visibility modifiers to help manage hiding. Java's visibility modifiers define four visibility levels, shown in the first column of the table below. Complete the table to specify the visibility of methods or fields declared with the different visibility levels.  

<table>
<thead>
<tr>
<th>visibility level</th>
<th>visible in the defining class?</th>
<th>visible in another class in the same package?</th>
<th>visible in a subclass in another package?</th>
<th>visible in a non-subclass in another package?</th>
</tr>
</thead>
<tbody>
<tr>
<td>public</td>
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<td>√</td>
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<tr>
<td>protected</td>
<td>√</td>
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<td>×</td>
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<tr>
<td>package</td>
<td>√</td>
<td>√</td>
<td>×</td>
<td>×</td>
</tr>
<tr>
<td>private</td>
<td>√</td>
<td>×</td>
<td>×</td>
<td>×</td>
</tr>
</tbody>
</table>

(b) Java provides a notion of package to help structure large systems. Recall that a package consists of a collection of classes, and has a hierarchical name.

i. What line of Java would you add to the top of the Student.java file to declare the Student class to be part of the package ed.informatics.cs1.studentdata?

```java
package ed.informatics.cs1.studentdata;  
```

[1 mark]

ii. What line of Java would you add to the top of another class in a different package, to be able to use the Student class (and no other classes) without writing long identifiers?

```java
import ed.informatics.cs1.studentdata.Student;  
```

[1 mark]

iii. What line of Java would you add to the top of another class in a different package, to be able to use all classes in the studentdata package, without writing long identifiers?

```java
import ed.informatics.cs1.studentdata.*;  
```

[1 mark]

iv. What is a disadvantage of using statements like those in ii and iii in your programs?

*Because long identifiers are not needed for class names after *import*, the location of a class in the following code may not be obvious.*

[1 mark]
Question 2
Consider the following Java code:

```java
abstract class FishShopMenu {
    public int price() { return 0; } // return price of menu item
    public abstract String toString(); // string name of menu item
}

class Fork extends FishShopMenu {
    public String toString() { return "Wooden fork"; }
}
```

Objects belonging to the class FishShopMenu represent items on the menu at a fish shop. The toString method provides the item name and the price method returns its price, as an integral number of pence.

i. How much does a wooden fork cost? [1 mark]

```
Zero pence (they’re free).
```

ii. Give the definition of a Haddock class, supposing that a haddock portion costs £1.85. [3 marks]

```java
class Haddock extends FishShopMenu {
    public int price() { return 185; }
    public String toString() { return "Haddock"; }
}
```

iii. What is wrong with the following definition of a Haggis class, supposing that a haggis portion costs £1.20? [1 mark]

```java
class Haggis extends FishShopMenu {
    public int price() { return 120; }
}
```

```
It doesn’t implement the toString method.
```

iv. The fish shop is running a special offer, which allows any item to be “super-sized” for only £0.80 extra. Give the definition of a Supersized class which implements this behaviour. The constructor should take a FishShopMenu object which is to be super-sized. [5 marks]

```java
class Supersized extends FishShopMenu {
    private FishShopMenu food;
    public Supersized(FishShopMenu food) {
        this.food = food;
    }
    public int price() {
        return food.price() + 80;
    }
    public String toString() {
        return "Supersized " + food.toString();
    }
}
```
Question 3

(a) *Infinity Software Systems* wish to display their corporate logo on their Web page in a Java applet. Their logo consists of 50 concentric open rectangles, in black on a white background, as shown below.

![Logo](image)

The centre of the logo is at co-ordinate (200,200). The width of the rectangle increases by 4 pixels and its height by 2 pixels in going from each rectangle to its nearest enclosing neighbour. Implement the `paint()` method for this applet. Recall that a `Graphics` context provides methods `setColor()`, `drawRect()` and `drawLine()` and that Java defines `Color.white` and `Color.black`. [5 marks]

```java
public void paint (Graphics g) {
    int x = 200;
    int y = 200;
    int width = 0;
    int height = 0;
    for (int i = 0 ; i < 50; i++) {
        x -= 2; y -= 1;
        width += 4; height += 2;
        g.setColor (Color.black);
        g.drawRect (x, y, width, height);
        g.setColor (Color.white);
        g.drawLine (x, y, x + width, y);
    }
}
```

(b) Some colours are pre-defined in Java, but others can be defined by the programmer. What is the method by which colours are specified? [2 marks]

It is possible to mix colours by specifying the amount of red, green and blue which should be used. The number 0 represents none at all and the maximum is 255. Thus for example (255, 0, 0) is red, (255, 255, 0) is yellow, and so forth.

(c) What are the attributes of a font which a Java programmer can specify? [3 marks]

Choice of font (e.g. *Times Roman* or *Courier*), style (e.g. *Italic*, *Bold* or *Plain*) and point size (e.g. 12, 14, 16, ...).
Question 4

(a) Describe the use of host names and port numbers in client/server systems. [2 marks]

A host name (such as scar.dcs.ed.ac.uk) identifies a particular machine on the network. A port number (such as 5055) identifies a particular service on a machine. A socket is made up of a host name and a port number.

(b) What role do proxy servers play in client/server systems? [2 marks]

The purpose of a proxy server is to increase reliability and reduce cost. It maintains a local cache of data which is accessed instead of the remote original.

(c) What are race conditions in client/server systems? [1 mark]

Difficult-to-diagnose errors which arise when the outcome of the interaction between two systems depends on their relative speed of operation.

(d) Complete the following client template code to enable it to communicate with a server which is listening on port 5055 of the machine java.ed.ac.uk.

```
import java.io.*;
import java.net.*;

class Client {
    public static void main (String[] args) throws IOException {
        Socket sock =
        new Socket("java.ed.ac.uk", 5055); [1 mark]

        // Communication has been established
        InputStreamReader is = new InputStreamReader (sock.getInputStream()); [1 mark]

        BufferedReader input = new BufferedReader(is);
        PrintWriter server = new PrintWriter (sock.getOutputStream()); [1 mark]

        server.println("Message sent"); [1 mark]
        server.flush();

        System.out.println("Reply: " + input.readLine()); [1 mark]
    }
}
```
Question 5

Consider the following container stuffing problem:

Parcel range in size from 1 to 10 units and containers can hold up to 10 units. Given a sequence $p_1, \ldots, p_n$ of parcels, find a way of stuffing them into containers so that the minimum number of containers is used to hold the parcels.

(a) One proposed solution is the greedy approach where we stuff containers one at a time always choosing the largest unstuffed parcel that will still fit in the container. When all the remaining parcels are too big to fit in the current container we go on to a new one, and so on. Can you find a sequence of parcels for which greedy approach fails to find a stuffing that minimises the number of containers used? Explain how your example causes the greedy approach to fail. [Hint: you don’t need to use parcels bigger than size 4.] [4 marks]

4, 4, 3, 3, 3, 3 This causes the greedy method to fail because the approach attempts to put the two size 4 parcels in one container; this wastes 2 units in the first container.

(b) Consider the following recursive program that solves the container stuffing problem. The method invocation stuffIt(s, parcel), where parcel is the vector of parcel sizes and s indicates we should solve the problem for the parcels between index s and the end of the vector. This invocation returns a Pair, where the containers instance variable counts the number of containers used and spare counts the amount of spare space left in the last container. After reading the program you should answer the questions below.

```java
public class Pair {
    public int containers;
    public int spare;

    public Pair () {
        containers = 0;
        spare = 0;
    }

    import java.util.*;

class Stuff {
    public static int size = 10;

    public static Pair add(Pair r, int p) {
        if (r.spare<p) {
            r.containers++; r.spare = size-p;
        } else { r.spare = r.spare-p;}
        return(r);
    }

    public static Pair min(Pair r1, Pair r2) {
        if (r1.containers<r2.containers ||
            (r1.containers==r2.containers
            && r1.spare>=r2.spare)) {
            return(r1);
        } else { return(r2); } }
}
public static Pair stuffIt(int start, Vector parcel) {
    Pair result;
    Integer first;
    if (start == parcel.size()) { .... } [A]
    start++;
    result = add(stuffIt(start, parcel),
                 ((Integer) parcel.elementAt(start-1)).intValue());
    for (int i = start; i < parcel.size(); i++) {
        first = (Integer) parcel.elementAt(i);
        parcel.setElementAt(parcel.elementAt(start-1),i);
        result = min(result, add(stuffIt(start, parcel), first.intValue()));
        parcel.setElementAt(first, i);
    }
    return(result);
}

i. In the program the line marked [A] is incomplete. Complete it in this box: [2 marks]

    return(new Pair());

iii. Provide a, reasonably accurate, estimate of the running time of the program for $n$ parcels. Justify your answer. [4 marks]

    The running time is approximately $O(n!)$ because the program really considers all possible sequences of parcels and calculates the smallest number of containers used over all the sequences.
Question 6

(a) The class below contains two Java methods, `eight()` and `add()`. Give the equivalent Java byte code which the Java compiler would produce for these methods. [5 marks]

```java
class Methods {
    static int eight() {
        return add(add(1, 3), 4);
    }
    static int add(int x, int y) {
        return x + y;
    }
}
```

**Method** int `eight()`  
0 `iconst_1`  
1 `iconst_3`  
2 `invokestatic` #2  
5 `iconst_4`  
6 `invokestatic` #2  
9 `ireturn`

**Method** int `add(int, int)`  
0 `iload_0`  
1 `iload_1`  
2 `iadd`  
3 `ireturn`

**Instructions needed:**
iconst—push int constant  
iload—load local variable  
iadd—add ints on stack  
ireturn—return int  
invokestatic—call method

(b) The following Java byte code method was written by hand by an inexperienced Java byte code programmer and will cause an error when it is executed. Identify the error by showing the intermediate steps in the execution of the method. [5 marks]

```java
Method int `six()`
0 `iconst_1`  
1 `iconst_2`  
2 `iconst_3`  
3 `iadd`  
4 `iadd`  
5 `iadd`  
6 `ireturn`
```

**Method** int `six()`  
0 `iconst_1`  
1 `iconst_2`  
2 `iconst_3`  
3 `iadd`  
4 `iadd`  
5 `iadd`  
6 `ireturn`

Method begins . . . :  
stack is empty  
push 1:  stack is 1.  
push 2:  stack is 2, 1.  
push 3:  stack is 3, 2, 1.  
add:  stack is 5, 1.  
add:  stack is 6.  
add:  **stack underflow error!**  
. . . method has exited abnormally
Question 7

(a) In contrast to locally compiled Java main programs, applets are restricted programs that can be downloaded from the Internet, for example. List three kinds of operation that a locally compiled program is allowed to carry out, but that a Java applet is not. [3 marks]

Any three from: filesystem accesses, networking operations, exit interpreter, spawn new processes or threads, dynamically load code, use AWT facilities, load or redefine core packages.

(b) Why are these sorts of sandboxing restrictions on applets considered to be a good idea? [2 marks]

Protect system from danger at execution time. Eliminate need for trust mechanisms applied to applet source and transmission.

(c) Give an example of a problem which a hostile applet could cause, despite sandboxing. [3 marks]

Most obvious answer would be something focused on denial of service.

(d) The following method is special for Java applications because it is never normally invoked by the programmer.

```
public static void main (String[] args)
```

Give the heading of a method which is similarly special for Java applets. As above, include the access control modifiers, the return type and the formal parameter list. [2 marks]

```
public void paint (Graphics G)
```


**Question 8**

(a) Explain what is meant by the *fetch-execute cycle* of a von Neumann machine.  

*Continuous cycle of: compute new PC value; fetch instruction from memory; and obey instruction.*

(b) Explain the distinction between i) a *machine instruction* and ii) a *micro-instruction.*  

*Machine instruction is assembly programmer’s view of the operations carried out by the processor. Micro-instruction is a lower-level internal view of operations actually executed in order to implement machine instructions.*

(c) The MIPS R2000 instruction `add $24, $4, $9` requests the processor to add the contents of Register 4 and Register 9, and place the result in Register 24. Using a register-transfer notation, or diagrams if you prefer, describe the sequence of operations that would be carried out by the datapath under the direction of the control unit.  

*PC ← PC+1; MAR ← PC
IR ← Memory[MAR]
24 ← 4+9*
Question 9

(a) Show the following equivalences are true using chains of logical equivalences.
   i. \(\neg(-P \land Q) \iff \neg Q \lor P\)

\[
\neg(-P \land Q) \iff \neg\neg P \lor \neg Q \\
\iff P \lor \neg Q \\
\iff \neg Q \lor P
\]

[2 marks]

ii. \(P \Rightarrow (Q \land P) \iff P \Rightarrow Q\)

\[
P \Rightarrow (Q \land P) \iff \neg P \lor (Q \land P) \\
\iff (\neg P \lor Q) \land (\neg P \lor P) \\
\iff (\neg P \lor Q) \land t \\
\iff \neg P \lor Q \\
\iff P \Rightarrow Q
\]

[2 marks]

(b) Consider the following truthtable for a 3 argument propositional operator \(X\).

<table>
<thead>
<tr>
<th>P</th>
<th>Q</th>
<th>R</th>
<th>(X(P, Q, R))</th>
</tr>
</thead>
<tbody>
<tr>
<td>t</td>
<td>t</td>
<td>f</td>
<td>f</td>
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<td>f</td>
</tr>
</tbody>
</table>

Write down the CNF (Conjunctive Normal Form) formula for \(X\) suggested by this truthtable.

\[
(P \lor Q \lor R) \land (P \lor \neg Q \lor R) \land (\neg P \lor \neg Q \lor \neg R)
\]

[2 marks]

(Question continues on next page)
(e) Use a semantic tree to show that the propositional formula \( ((P \lor Q) \Rightarrow Q) \Rightarrow Q \) is not a tautology. If you have a choice of formulas to discharge, discharge first the formula closest to the tree root. Explicitly state a counter-example truth assignment suggested by the tree.

\[
* f: ((P \lor Q) \Rightarrow Q) \Rightarrow Q \\
* t: (P \lor Q) \Rightarrow Q \\
f: Q \\
f: P \otimes \\
f: Q \\
\]

Counter-example truth-assignment is \( \{ P \mapsto f, Q \mapsto f \} \).

Marking:
2 marks for correct rule applications
1 mark for closing contradictory path
1 mark for correctly reading off counter-example from tree.

[4 marks]
**Question 10**

(a) Consider the static Java method

```java
public static int sPower(int a, int n) {
    if (n == 0)
        return a;
    else
        return sPower(a, n-1) * sPower(a, n-1);
}
```

Show by induction on \( n \) that \( \forall n : \mathbb{N}. sPower(a, n) = a^{2^n} \)

where \( \mathbb{N} \) is the non-negative integers \( \{0, 1, 2, \ldots\} \).

i. How does the base case argument go?

**The base case is:**

\[ sPower(a, 0) = a^{2^0} \]

Both sides are obviously equal to \( a \).

[1 mark]

ii. For the step case, what is the inductive hypothesis and what is the statement to be shown?

**The inductive hypothesis is:**

\( sPower(a, k) = a^{2^k} \)

and

\( sPower(a, k + 1) = a^{2^{(k+1)}} \)

is to be shown. where \( k \geq 0 \).

[2 marks]

iii. What is the proof of the step case?

\[
\begin{align*}
    sPower(a, k + 1) &= sPower(a, k) * sPower(a, k) \\
                     &= a^{2^k} * a^{2^k} \\
                     &= a^{2^{(k+1)}}
\end{align*}
\]

by definition of \( sPower \)

by I.H.

by arithmetic

[2 marks]
(b) Complete the the \texttt{requires} (precondition), \texttt{ensures} (postcondition) and \texttt{loop invariant} assertions for the following Java method which tests if integer \texttt{i} is contained in integer array \texttt{seq}:

\begin{verbatim}
//@ requires

//@ seq ! = null;

//@ ensures
//@ \result \iff \exists \ \texttt{k} \in \mathbb{Z} \mid 0 \leq \texttt{k} < \texttt{seq}.length \land \texttt{i} = \texttt{seq}[\texttt{k}];

static boolean member(int i; int[] seq) {
  boolean val = false;
  // @ loop_invariant
  // @ val <=>
  //@ (\exists \texttt{k}; 0 \leq \texttt{k} < \texttt{j} \land \texttt{i} = \texttt{seq}[\texttt{k}]);

  for (int j = 0; j != seq.length; j++) {
    if (i == seq[j]) val = true;
  }
  return val;
}
\end{verbatim}

Recall, a \texttt{loop invariant} assertion concerns the state of the program just before each evaluation of the loop termination test. The special specification variable \texttt{\result} is used in \texttt{ensures} statements to refer to the return value of a method.

Write your assertions using the extended Java-like syntax illustrated in class, or, if you prefer, more logic-like syntax.